

Proof techniques

Similar lists have been circulating around the net for decades. The original was written by Dan Angluin and published in SIGACT News, Winter-Spring 1983, Volume 15 #1. ---Margaret Fleck

Proof by example

The author gives only the case $n = 2$ and suggests that it contains most of the ideas of the general proof.

Proof by intimidation

``Trivial" or ``obvious."

Proof by exhaustion

An issue or two of a journal devoted to your proof is useful.

Proof by omission

``The reader may easily supply the details", ``The other 253 cases are analogous"

Proof by obfuscation

A long plotless sequence of true and/or meaningless syntactically related statements.

Proof by wishful citation

The author cites the negation, converse, or generalization of a theorem from the literature to support his claims.

Proof by funding

How could three different government agencies be wrong? Or, to play the game a different way: how could anything funded by those bozos be correct?

Proof by democracy

A lot of people believe it's true: how could they all be wrong?

Proof by market economics

Mine is the only theory on the market that will handle the data.

Proof by eminent authority

``I saw Ruzena in the elevator and she said that was tried in the 70's and doesn't work."

Proof by cosmology

The negation of the proposition is unimaginable or meaningless. Popular for proofs of the existence of God and for proofs that computers cannot think.

Proof by personal communication

``Eight-dimensional colored cycle stripping is NP-complete [Karp, personal communication]."

Proof by reference to talk

``At the special NSA workshop on computer vision, Binford proved that SHGC's could be recognized in polynomial time."

Proof by reduction to the wrong problem

``To see that infinite-dimensional colored cycle stripping is decidable, we reduce it to the halting problem."

Proof by reference to inaccessible literature

The author cites a simple corollary of a theorem to be found in a privately circulated memoir of the Icelandic Philological Society, 1883. This works even better if the paper has never been translated from the original Icelandic.

Proof by ghost reference

Nothing even remotely resembling the cited theorem appears in the reference given. Works well in combination with proof by reference to inaccessible literature.

Proof by forward reference

Reference is usually to a forthcoming paper of the author, which is often not as forthcoming as at first.

Proof by importance

A large body of useful consequences all follow from the proposition in question.

Proof by accumulated evidence

Long and diligent search has not revealed a counterexample.

Proof by mutual reference

In reference A, Theorem 5 is said to follow from Theorem 3 in reference B, which is shown to follow from Corollary 6.2 in reference C, which is an easy consequence of Theorem 5 in reference A.

Proof by metaproof

A method is given to construct the desired proof. The correctness of the method is proved by any of these techniques. A strong background in programming language semantics will help here.

Proof by picture

A more convincing form of proof by example. Combines well with proof by omission.

Proof by flashy graphics

Also known as the Jaberwocky method. Only a really powerful result could underly such an awesome sound and light show. "Products are for people who don't have presentations."

Proof by misleading or uninterpretable graphs

Almost any curve can be made to look like the desired result by suitable transformation of the variables and manipulation of the axis scales. Common in experimental work.

Proof by vehement assertion

It is useful to have some kind of authority relation to the audience, so this is particularly useful in classroom settings.

Proof by repetition

Otherwise known as the Bellman's proof: "What I say three times is true."

Proof by appeal to intuition

Cloud-shaped drawings frequently help here.

Proof by vigorous handwaving

Works well in a classroom, seminar, or workshop setting.

Proof by semantic shift

Some of the standard but inconvenient definitions are changed for the statement of the result.

Proof by cumbersome notation

Best done with access to at least four alphabets, special symbols, and the newest release of LaTeX.

Proof by abstract nonsense

A version of proof by intimidation. The author uses terms or theorems from advanced mathematics which look impressive but are only tangentially related to the problem at hand. A few integrals here, a few exact sequences there, and who will know if you really had a proof?

Disproof by finding a bad apple

One bad apple spoils the whole bunch. Among the many proponents of this theory, we have found one who is obviously loony; so we can discredit the entire theory. (Often used in political contexts.)

Disproof by slippery slope (or thin end of wedge, if you are British)

If we accepted [original proposal], we'd have to accept [slightly modified proposal], and eventually this would lead to [radically different and clearly objectionable proposal].

Disproof by ``not invented here''

We have years of experience with this equipment at MIT and we have never observed that effect.